

# Properties of Geometrical Figures – Question Set

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## 1. Straight-Line & Vertically Opposite Angles

**Q1** Two adjacent angles form a straight line. One angle is  $38^\circ$ . Find the other.

**Q2** Vertically opposite angles at a point are  $5x^\circ$  and  $3x + 30^\circ$ . Solve for  $x$ .

**Q3** Around a point the angles shown are  $112^\circ, 87^\circ, y^\circ$  and  $z^\circ$ . Find  $y$  and  $z$ .

## 2. Parallel Lines

**Q4** A transversal cuts two parallel lines. One corresponding angle is  $64^\circ$ . Find (a) the alternate interior angle, (b) the co-interior angle adjacent to it.

**Q5** Lines  $p \parallel q$ . The angle between the transversal and  $p$  on the outside is  $3k^\circ$ . The alternate interior angle on  $q$  is  $2k + 20^\circ$ . Determine  $k$ .

## 3. Triangles

**Q6** Find the third angle of a triangle with angles  $53^\circ$  and  $67^\circ$ .

**Q7** In  $\triangle ABC$ , exterior angle at  $C$  is  $148^\circ$  and interior angle at  $A$  is  $62^\circ$ . Calculate interior angle at  $B$ .

**Q8** Triangle  $XYZ$  is isosceles with  $XY = XZ$  and vertex angle  $Y = 46^\circ$ . Find the base angles.

## 4. Quadrilaterals

**Q9** Quadrilateral  $PQRS$  has three interior angles  $92^\circ, 105^\circ, 88^\circ$ . Find the fourth.

**Q10** A kite has equal sides 9 cm and unequal angles at its apex  $54^\circ$ . Find each base angle.

## 5. Regular Polygons

**Q11** What is one exterior angle of a regular dodecagon (12-gon)?

**Q12** Each interior angle of a regular polygon is  $165^\circ$ . How many sides does it have?

## 6. Mixed Reasoning

**Q13** The diagram shows two intersecting lines and a pair of parallel lines (information on your copy). Express, in terms of  $x$ , the value of the angle marked  $y$ . \*[Provide your own labelled sketch if required.]\*

**Q14** Explain why the interior angles of any triangle sum to  $180^\circ$  using a parallel-line argument.

## Challenge Question

**Q1** A regular  $n$ -gon has an interior angle which is three times its exterior angle.

- Form an equation linking the interior and exterior angles of the polygon and solve for  $n$ .
- Determine the size of each interior and exterior angle.